

Table 1 : Table of Hydrodynamic Coefficients for Heaving

Heaving	OSM	Present(NSM)
a_{33}	$\int (w/g + \rho M_1) dx$	$\int (w/g + \rho M_1) dx + U/\omega_e^2[\rho N_1]$
b_{33}	$\int \rho N_1 dx - U[\rho M_1]$	$\int \rho N_1 dx - U[\rho M_1]$
c_{33}	$\int 2\rho g y_w dx$	$\int 2\rho g y_w dx$
a_{35}	$-\int (w/g + \rho M_1) X dx$	$-\int (w/g + \rho M_1) X dx - U/\omega_e^2 \int \rho N_1 dx$ $- U/\omega_e^2[\rho N_1 X] + (U/\omega_e)^2[\rho M_1]$
b_{35}	$-\int \rho N_1 X dx + U \int \rho M_1 dx + U[\rho M_1 X]$	$-\int \rho N_1 X dx + U \int \rho M_1 dx + U[\rho M_1 X]$ $+ (U/\omega_e)^2[\rho N_1]$
c_{35}	$-\int 2\rho g y_w X dx + U \int \rho N_1 dx - U^2[\rho M_1]$	$-\int 2\rho g y_w X dx$

F_{w3c} F_{w3s}	OSM	$\zeta_a \int 2\rho g y_w c_1 c_2 \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega \zeta_a \int \rho N_1 c_1 c_2 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_1 c_1 c_2 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_1 c_1 c_2 \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} \right]$
	NSM	$\zeta_a \int 2\rho g y_w c_1 c_2 \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega_e \zeta_a \int \rho N_{10} c_1 c_2 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_{10} c_1 c_2 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_{10} c_1 c_2 \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} \right]$ $+ U \zeta_a \left[\rho N_{10} c_1 c_2 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} \right]$
	Present	$\zeta_a \int \int_C \rho g \cos(k y \sin \chi) dy \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega_0^2 \zeta_a \int \rho M_{41} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega_0^2 / \omega_e \zeta_a \int \rho N_{41} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega_0 / \omega_e U \zeta_a \left[\rho N_{41} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} \right]$ $+ \omega_0 U \zeta_a \left[\rho M_{41} \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} \right]$

여기서 NSM의 과강제력에 있어 M_{10}, N_{10} 은 과주파수 ω_0 의 유체력이다.

또, $X = x - x_G$, $\bar{X} = x - x_G$ (과랑하중의 경우 $\bar{X} = x - x_1$), σ : 단면계수,

$k^* = k \cos \chi$, y_w : x 단면의 수선의 반폭

$$c_1 = \sin(k y_w \sin \chi) / (k y_w \sin \chi), \quad \chi \neq n\pi$$

$$= 1.0, \quad \chi = n\pi, \quad n = 0, 1, 2, \dots$$

$$c_2 = e^{-k\sigma d}$$

Table 2 : Table of Hydrodynamic Coefficients for Pitching

Heaving	OSM	Present(NSM)
a_{53}	$-\int (w/g + \rho M_1) \bar{X} dx$	$-\int (w/g + \rho M_1) \bar{X} dx + U/\omega_e^2 \int \rho N_1 dx$ $- U/\omega_e^2 [\rho N_1 \bar{X}]$
b_{53}	$-\int \rho N_1 \bar{X} dx - U \int \rho M_1 dx + U[\rho M_1 \bar{X}]$	$-\int \rho N_1 \bar{X} dx - U \int \rho M_1 dx + U[\rho M_1 \bar{X}]$
c_{53}	$-\int 2\rho g y_w \bar{X} dx$	$-\int 2\rho g y_w \bar{X} dx$
a_{55}	$\int (w/g + \rho M_1) X \bar{X} dx$	$\int (w/g + \rho M_1) X \bar{X} dx + U/\omega_e^2 \int \rho N_1 (\bar{X} - X) dx$ $+ (U/\omega_e)^2 \int \rho M_1 dx + U/\omega_e^2 [\rho N_1 X \bar{X}]$ $- (U/\omega_e)^2 [\rho M_1 X]$
b_{55}	$\int \rho N_1 X \bar{X} dx - U \int \rho M_1 (\bar{X} - X) dx$ $- U[\rho M_1 X \bar{X}]$	$\int \rho N_1 X \bar{X} dx - U \int \rho M_1 (\bar{X} - X) dx$ $+ U^2/\omega_e^2 \int \rho N_1 dx - U[\rho M_1 X \bar{X}]$ $- U^2/\omega_e^2 [\rho N_1 \bar{X}]$
c_{55}	$\int 2\rho g y_w X \bar{X} dx - U \int \rho N_1 X dx$ $- U^2 \int \rho M_1 dx + U^2[\rho M_1 X]$	$\int 2\rho g y_w X \bar{X} dx$

	OSM	$\zeta_a \int 2\rho g y_w c_1 c_2 \bar{X} \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$ $+ \omega \zeta_a \int \rho N_1 c_1 c_2 \bar{X} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_1 c_1 c_2 \bar{X} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_1 c_1 c_2 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} \right]$ $+ \omega U \zeta_a \int \rho M_1 c_1 c_2 \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$
M_{w5c} M_{w5s}	NSM	$\zeta_a \int 2\rho g y_w c_1 c_2 \bar{X} \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$ $+ \omega_e \zeta_a \int \rho N_{10} c_1 c_2 \bar{X} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_{10} c_1 c_2 \bar{X} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_{10} c_1 c_2 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} \right]$ $+ \omega U \zeta_a \int \rho M_{10} c_1 c_2 \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ U \zeta_a \left[\rho N_{10} c_1 c_2 \bar{X} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} \right]$ $+ U \zeta_a \int \rho N_{10} c_1 c_2 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$
	Present	$\zeta_a \int \int \rho g \cos(k y \sin \chi) dy \bar{X} \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$ $+ \omega_0^2 \zeta_a \int \rho M_{41} \bar{X} \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} dx$ $+ \omega_0 / \omega_e U \zeta_a \int \rho N_{41} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega_0^2 / \omega_e \zeta_a \int \rho N_{41} \bar{X} \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega_0 U \zeta_a \int \rho M_{41} \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega_0 / \omega_e U \zeta_a \left[\rho N_{41} \bar{X} \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} \right]$ $+ \omega_0 U \zeta_a \left[\rho M_{41} \bar{X} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} \right]$

Table 3. Table of hydrodynamic Coefficients for Swaying

SWAY	OSM	Present(NSM)
a_{22}	$\int (w/g + \rho M_2) dx$	$\int (w/g + \rho M_2) dx + U/\omega_e^2 [\rho N_2]$
b_{22}	$\int \rho N_2 dx - U[\rho M_2]$	$\int \rho N_2 dx - U[\rho M_2]$
c_{22}	0	0
a_{24}	$\int \rho M_2 l_\eta' dx$	$\int \rho M_2 l_\eta' dx + U/\omega_e^2 \rho N_2 l_w'$
b_{24}	$\int \rho N_2 l_w' dx - U[\rho M_2 l_\eta']$	$\int \rho N_2 l_w' dx - U[\rho M_2 l_\eta']$
c_{24}	0	0
a_{26}	$\int (w/g + \rho M_2) X dx$	$\int (w/g + \rho M_2) X dx + U/\omega_e^2 \int \rho N_2 dx - U^2/\omega_e^2 [\rho M_2]$
b_{26}	$\int \rho N_2 X dx - U \int \rho M_2 dx - U[\rho M_2 X]$	$\int \rho N_2 X dx - U \int \rho M_2 dx - U[\rho M_2 X]$
c_{26}	$- U \int \rho N_2 dx + U^2 [\rho M_2]$	$0 - U^2/\omega_e^2 [\rho N_2]$

	OSM	$\zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) dz \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega \zeta_a \int \rho N_2 c_3 \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_2 c_3 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_2 c_3 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} \right]$
F_{w2c}	NSM	$\zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) dz \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega \zeta_a \int \rho N_2 c_3 \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_2 c_3 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_2 c_3 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} \right]$
F_{w2s}	Present	$\zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) dz \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega_0^2 \zeta_a \int \rho M_{42} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega_0^2 / \omega_e \zeta_a \int \rho N_{42} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega_0 / \omega_e U \zeta_a \left[\rho N_{42} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} \right]$ $+ \omega_0 U \zeta_a \left[\rho M_{42} \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} \right]$

여기에서 $c_3 = \sin \chi \cdot e^{-kd/2}$

Table 4. : Table of hydrodynamic Coefficients for Yawing

YAW	OSM	Present(NSM)
a_{62}	$\int \rho(w/g + \rho M_2) \bar{X} dx$	$\int \rho(w/g + \rho M_2 \bar{X}) dx - U/\omega_e^2 \int \rho N_2 dx$
b_{62}	$\int \rho N_2 \bar{X} dx + U \int \rho M_2 dx - U[\rho M_2 \bar{X}]$	$+ U/\omega_e^2 [\rho N_2 \bar{X}] \int \rho N_2 \bar{X} dx + U \int \rho M_2 dx - U[\rho M_2 X]$
c_{62}	0	0
a_{64}	$\int \rho M_2 l'_\eta \bar{X} dx$	$\int \rho M_2 l'_\eta X dx - U/\omega_e^2 \int \rho N_2 l'_w dx + \omega_e^2 [\rho N_2 X l'_w]$
b_{64}	$U \int \rho N_2 l'_\eta dx - U[\rho M_2 l'_\eta \bar{X}] + \int \rho N_2 l'_w \bar{X} dx$	$U \int \rho M_2 l'_\eta dx - U \rho M_2 l'_\eta X + \int \rho N_2 l'_w X dx$
c_{64}	0	0
a_{66}	$\int (w/g + \rho M_2 \bar{X} \bar{X}) dx$	$\int (w/g + \rho M_2) X \bar{X} dx + U/\omega_e^2 \int \rho N_2 (\bar{X} - X) dx$ $+ (U/\omega_e)^2 \int \rho M_2 dx - U/\omega_e^2 [\rho N_2 X \bar{X}]$
b_{66}	$\int \rho N_2 X \bar{X} dx - U \int \rho M_2 (\bar{X} - X) dx$	$\int \rho N_2 X \bar{X} dx - U \int \rho M_2 (\bar{X} - X) dx$ $+ (U/\omega_e)^2 \int \rho N_2 dx - U[\rho M_2 X \bar{X}] - (U/\omega_e)^2 [\rho N_2 \bar{X}]$
c_{66}	$- U \int \rho N_2 X dx - U^2 \int \rho M_2 dx + U^2 [\rho M_2 X]$	0

	OSM	$\begin{aligned} & \zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) dz \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) dx \\ & + \omega \zeta_a \int \rho N_2 c_3 \bar{X} \left(\begin{array}{c} \cos k^* x \\ \sin k^* x \end{array} \right) dx \\ & + \omega \omega_e \zeta_a \int \rho M_2 c_3 \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) dx \\ & + \omega U \zeta_a \int \rho M_2 c_3 \left(\begin{array}{c} \cos k^* x \\ \sin k^* x \end{array} \right) dx \\ & + \omega / \omega_e U \zeta_a \int \rho N_2 c_3 \left(\begin{array}{c} -\sin k^* x \\ \cos k^* x \end{array} \right) dx \end{aligned}$
F_{w2c}	NSM	$\begin{aligned} & \zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) dz \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) dx \\ & + \omega \zeta_a \int \rho N_2 c_3 \bar{X} \left(\begin{array}{c} \cos k^* x \\ \sin k^* x \end{array} \right) dx \\ & + \omega \omega_e \zeta_a \int \rho M_2 c_3 \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) dx \\ & + \omega U \zeta_a \int \rho M_2 c_3 \left(\begin{array}{c} \cos k^* x \\ \sin k^* x \end{array} \right) dx \\ & + \omega / \omega_e U \zeta_a \int \rho N_2 c_3 \left(\begin{array}{c} -\sin k^* x \\ \cos k^* x \end{array} \right) dx \\ & + \omega U \zeta_a \left[\rho M_2 c_3 \bar{X} \left(\begin{array}{c} -\cos k^* x \\ -\sin k^* x \end{array} \right) \right] \\ & + \omega / \omega_e U \zeta_a \left[\rho N_2 c_3 \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) \right] \end{aligned}$
F_{w2s}	Present	$\begin{aligned} & \zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) dz \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) dx \\ & + \omega_0^2 \zeta_a \int \rho M_{42} \bar{X} \left(\begin{array}{c} \cos k^* x \\ \sin k^* x \end{array} \right) dx \\ & + \omega_0 / \omega_e U \zeta_a \int \rho N_{42} \left(\begin{array}{c} -\cos k^* x \\ -\sin k^* x \end{array} \right) dx \\ & + \omega_0^2 / \omega_e \zeta_a \int \rho N_{42} \bar{X} \left(\begin{array}{c} -\sin k^* x \\ \cos k^* x \end{array} \right) dx \\ & + \omega_0 U \zeta_a \int \rho M_{42} \left(\begin{array}{c} -\sin k^* x \\ \cos k^* x \end{array} \right) dx \\ & + \omega_0 / \omega_e U \zeta_a \left[\rho N_{42} \bar{X} \left(\begin{array}{c} \cos k^* x \\ \sin k^* x \end{array} \right) \right] \\ & + \omega_0 U \zeta_a \left[\rho M_{42} \bar{X} \left(\begin{array}{c} \sin k^* x \\ -\cos k^* x \end{array} \right) \right] \end{aligned}$

Table 5. : Table of hydrodynamic Coefficients for Rolling

ROLL	OSM	Present(NSM)
a_{42}	$\int \rho M_2 l'_\eta dx$	$\int \rho M_2 l'_\eta dx + U/\omega_e^2[\rho N_2 l'_w]$
b_{42}	$\int \rho N_2 l'_w dx - U[\rho M_2 l'_\eta]$	$\int \rho N_2 l'_w dx - U[\rho M_2 l'_\eta]$
c_{42}	0	0
a_{44}	$\int (i_{xx} + \rho M_3) dx + U/\omega_e^2[\rho N_3]$	$\int (i_{xx} + \rho M_3) dx + U/\omega_e^2[\rho N_3]$
b_{44}	$\int \rho N_3 dx - U[\rho M_3]$	$\int \rho N_3 dx - U[\rho M_3]$
c_{44}	$\int w \cdot g m dx = WGM$	$\int w \cdot g m dx = WGM$
a_{46}	$\int \rho M_2 l'_\eta X dx$	$\int \rho M_2 l'_\eta X dx + U/\omega_e^2 \int \rho N_2 l'_w dx - U^2/\omega_e^2[\rho M_2 l'_\eta]$ $+ U/\omega_e^2[\rho N_2 l'_w X]$
b_{46}	$\int \rho N_2 l'_w X dx - U \int \rho M_2 l'_w dx - U[\rho M_2 l'_\eta X]$	$\int \rho N_2 l'_w X dx - U \int \rho M_2 l'_w dx - U[\rho M_2 l'_\eta X]$ $- U^2/\omega_e^2[\rho N_2 l'_w]$
c_{46}	$- U \int \rho N_2 l'_w dx + U^2[\rho M_2 l'_\eta]$	0

F_{w4c} F_{w4s}	OSM	$\zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) \cdot \{y dy - (z - z_G) dz\} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega \zeta_a \int \rho N_2 l_w' c_3 \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_2 l_\eta' c_3 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_2 l_\eta' c_3 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} \right]$
	NSM	$\zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) \cdot \{y dy - (z - z_G) dz\} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega \zeta_a \int \rho N_2 l_w' c_3 \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega \omega_e \zeta_a \int \rho M_2 l_\eta' c_3 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} dx$ $+ \omega U \zeta_a \left[\rho M_2 l_\eta' c_3 \begin{pmatrix} -\cos k^* x \\ -\sin k^* x \end{pmatrix} \right]$ $+ \omega / \omega_e U \zeta_a \rho N_2 c_3 \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix}$
	Present	$\zeta_a \int \int_C \rho g e^{-kz} \sin(ky \sin \chi) \cdot \{y dy - (z - z_G) dz\} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega_0^2 \zeta_a \int \rho M_{43} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} dx$ $+ \omega_0^2 / \omega_e \zeta_a \int \rho N_{43} \begin{pmatrix} -\sin k^* x \\ \cos k^* x \end{pmatrix} dx$ $+ \omega_0 / \omega_e U \zeta_a \left[\rho N_{43} \begin{pmatrix} \cos k^* x \\ \sin k^* x \end{pmatrix} \right]$ $+ \omega_0 U \zeta_a \left[\rho M_{43} \begin{pmatrix} \sin k^* x \\ -\cos k^* x \end{pmatrix} \right]$